

THE PAPUA NEW GUINEA UNIVERSITY OF TECHNOLOGY

Department of Mechanical Engineering

ME223 Fluid Mechanics for Mechanical Engineering

Final Examination 2<sup>nd</sup> Year Degree

Semester 2, Year 2024

Time Allowed: 2 hours

Wednesday, October 23, 2024 – 08:20

**INSTRUCTION FOR STUDENTS**

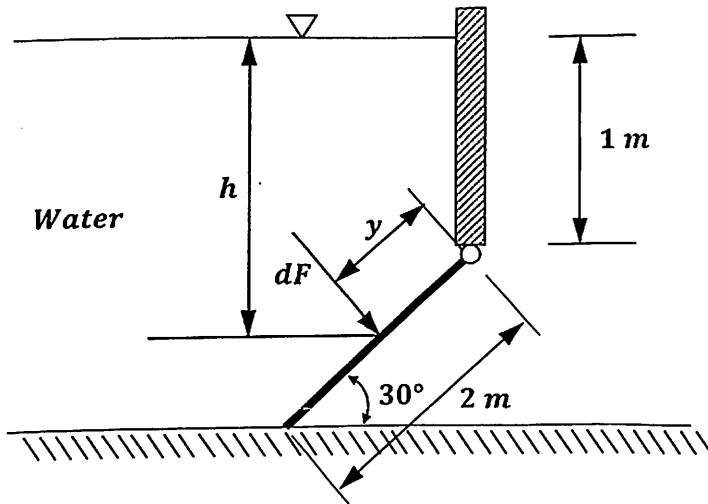
- (1) YOU HAVE 10 MINUTES TO READ THE PAPER. DO NOT WRITE ANYTHING DURING THIS TIME.
- (2) CHECK YOUR QUESTION PAPER HAS 7 PAGES.
- (3) TOTAL NUMBER OF QUESTIONS – FOUR (4). ANSWER ALL QUESTIONS
- (4) SHOW YOUR WORK CLEARLY. FOR FULL CREDIT SHOW ALL STEPS.
- (5) NOTES AND TEXT BOOKS ARE NOT ALLOWED. CALCULATORS ARE PERMITTED IN THE EXAMINATION ROOM.
- (6) WRITE YOUR NAME AND STUDENT NUMBER CLEARLY ON THE FRONT OF THE ANSWER BOOKLET. DO IT NOW.
- (7) START EACH QUESTION ON A NEW PAGE AND SHOW ALL YOUR WORK IN THE ANSWER BOOK PROVIDED.
- (8) TOTAL MARKS: 40
- (9) MARKING SCHEME:

|            |          |
|------------|----------|
| QUESTION 1 | 5 MARKS  |
| QUESTION 2 | 5 MARKS  |
| QUESTION 3 | 14 MARKS |
| QUESTION 4 | 16 MARKS |

**ALL ANSWERS MUST BE WRITTEN IN INK.**

**QUESTION 1**

Determine the total force by integration due to water pressure on the inclined surface shown in the diagram below. The surface is hinge at the top and is 3 m wide.



**NOTE:** The total force is normal to the gate and may be found by integrating the pressure over the surface.

**QUESTION 2**

A spherical balloon of diameter 1.5 m and total mass 1.2 kg, is released in the atmosphere. Assuming that the balloon does not expand and that temperature lapse rate in the atmosphere is  $\lambda = 0.0065 \text{ K/m}$ , determine the height ( $Z$ ) above sea-level to which the balloon will rise. Atmospheric temperature and pressure at sea-level are  $15^\circ\text{C}$  and 101 kPa respectively; for air,  $R = 287 \text{ J/kgK}$  (gas constant). Use the information provided above to calculate the following densities;

1. Density of balloon,  $\rho = \text{_____ kg/m}^3$
2. Density of the air at  $15^\circ\text{C}$  and 101 kPa,  $\rho_o = \text{_____ kg/m}^3$

Now, use the above densities and the following equations provided to calculate height ( $Z$ );

- If the temperature lapse rate is constant, then  $T = T_o - \lambda Z$ ,
- $P/P_o = \exp(-gZ/RT)$  also  $\ln \frac{P}{P_o} = \frac{g}{R\lambda} \ln \frac{T_o - \lambda Z}{T_o}$
- Also  $\ln \frac{\rho}{\rho_o} = \ln \frac{P}{P_o} - \ln \frac{T}{T_o} = \left( \frac{g}{R\lambda} - 1 \right) \ln \left( \frac{T_o - \lambda Z}{T_o} \right)$

**QUESTION 3**

A uniform, closed cylinder buoy, 1.5 m high, 1.0 m diameter, and of mass 80 kg is to float with its axis vertical in sea water of density 1026 kg/m<sup>3</sup>. A body of mass 10 kg is attached to the centre of the top surface of the buoy as shown on the diagram below.

Show that, if the buoy floats freely, initial instability will occur.

**TIPS on answering Q3 refer to the diagram and information provided below:**

- Take moments of mass about horizontal axis through O to find OG

$$\therefore OG = \text{_____} m$$

- For vertical equilibrium, use buoyance = weight to find  $h$

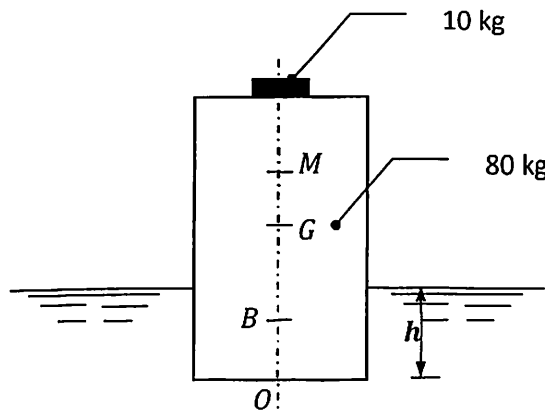
- Use Second moment of the centroidal axes or  $Ak^2$  of a circle about a centroidal axis is given as  $(Ak^2)_{CC} = \pi d^4 / 64$  to find BM.

Where:

$$A = \text{cross sectional area}; k = \text{radius of gyration}; BM = \frac{Ak^2}{V}; V = \frac{\pi d^2}{4} h \text{ (vol. submerged)}$$

$$\therefore BM = \text{_____} m$$

- Now, find GM as per the **NOTES** below and draw your conclusion.

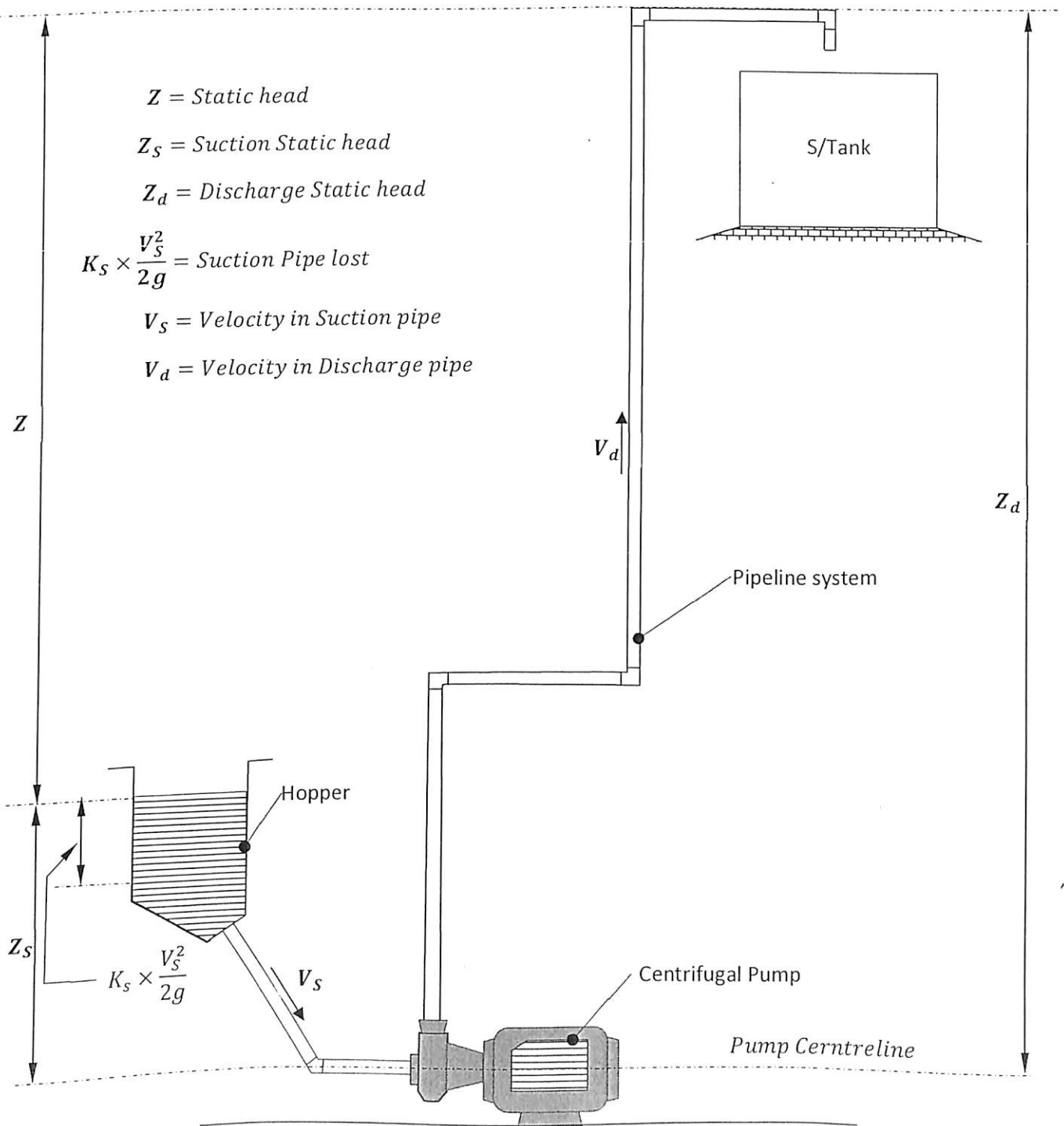


**NOTES:**

1. For stability,  $GM = OB + BM - OG = \text{positive for stability i. e. } M \text{ has to be above } G$
2. For instability,  $GM = OB + BM - OG = \text{negative for instability i. e. } M \text{ is below } G$

**QUESTION 4**

You were asked to design a pipeline system to convey process water to a storage tank. Your task is to design and select a pump from the pump performance curve that will overcome all the system resistance from the entire installations to pump process water from the hopper to the storage tank via the centrifugal pump. The pump will be gravity fed from a hopper and be arranged generally as shown on the diagram below.



You are also being told that a heavy-duty process water pump is to be selected for the following duty:

- *Static discharge head ( $Z_d$ ) = 20 metres*
- *Suction head ( $Z_s$ ) = 1 metre (positive)*
- *Length of pipeline = 100 metres*
- *Valves and fittings =  $5 \times 90^\circ$  long radius bends*
- *Flowrate of process water,  $Q_p = 176.2 \text{ m}^3/\text{hr} = 49 \text{ L/s}$*
- *Pipe diameter,  $D_p = 150 \text{ mm}$*
- *Assumed,  $g = 9.81 \text{ m/s}^2$*

Calculate the total pressure drop in metre (m) head of water against the flow rate in L/s given and selected the appropriate pump and specify the model, efficiency and motor speed in rpm from the pump performance curve attached.

**a) Process Water Velocity in m/s in Pipeline**

A 150mm diameter steel pipe is selected for the system, what is the process water velocity  $V_p$  (process water velocity in m/s)?

Calculate  $V_p$  in m/s to the nearest whole number i.e.  $V_p = \text{_____} \text{ m/s}$

**b) Friction head  $H_f$  for the pipeline**

The equivalent length of valves and fittings head losses is given as 3.35 metre each. Use this information to determine the equivalent length  $L$  of the pipeline system and calculate the friction head in metre head of water. The value  $f = 0.017$  is given for the Darcy's equation for friction head. State the Darcy's equation and calculate both  $L$  and  $H_f$ .

**c) Loss in discharge pipe enlargement**

The pump discharge is found to be 100mm diameter. Therefore a pipe transition piece is required in this case to enlarge the discharge to the 150mm pipeline size. The Head loss in this case using an enlargement included angle of  $30^\circ$  and through interpolation,  $K_e = 0.55$ . You now need to calculate the velocities in the transition piece and use the correct formula to calculate the corresponding Head loss in m of water  $H_e$ :

**d) Loss at pipe discharge**

Under the normal open discharge conditions, the velocity head at the pump discharge must be added to the required total head. State the formula for the velocity head and calculate the head  $H_d$  in m of water.

**e) Loss of head at entrance to suction pipe**

The suction (inlet) pipe is similar to the discharge diameter of 150 mm. Assuming the hopper would be fitted with a flush type connection, calculate the head loss  $H_{et}$ , where  $k = 0.5$ .

**f) Total dynamic head on the pump**

Under the normal open discharge conditions, the velocity head at the pump discharge must be added to the required total head  $H_m$ .

$H_m = Z + H$ , where  $Z$  is static head and  $H$  is the sum of all losses

**g) Equivalent water total dynamic head**

Using Correction factor (HR) as 0.89. The total head of equivalent water ( $H_w$ ) is therefore calculated.

$$H_w = \frac{H_m}{HR}$$

**h) Pump Selection**

The pump can now be selected, using the required flow rate of 49 L/s and total head of  $H_w$  of equivalent water from the pump performance curve. Plot the pump performance curves provided and select the followings as your answer:

- a) Pump Efficiency and RPM?
- b) Pump Model?

