

THE PAPUA NEW GUINEA UNIVERSITY OF TECHNOLOGY

MECHANICAL ENGINEERING

FIRST SEMESTER EXAMINATION - 2023

**Control Engineering ME 412
June 5th, 2023**

MAXIMUM MARKS: 40

TIME ALLOWED: 2 HOURS

INSTRUCTIONS FOR CANDIDATES:

1. You have 10 minutes to read the paper. You must not begin writing during this time.
2. Answer all the **FOUR** questions. Marks on each part of the questions are indicated in the bracket.
3. Use only ink. Do not use pencil or writing except on drawing and sketches.
4. All answers must be written in the answer book provided. No other written material will be accepted.
5. Write your **name** and **ID number** clearly on the front page of the answer booklet provided. **Do it now!**
6. Use of Calculator in the exam room is permitted. Notes, digital phones and textbooks are not allowed. Required property values are provided in the question paper.

Question 1. Write down and discuss the Laplace Transform for the following functions:

- 1.1. Exponential Function 3 Marks
- 1.2. Step Function 2 Marks
- 1.3. Ramp Function 2 Marks
- 1.3. Impulse Function 3 Marks

Question 2. Find the inverse Laplace transform of: the following complex functions:

2.1. $F(s) = \frac{s^3 + 3s^2 + 7s + 5}{s^2 + 2s - 3}$. Use the attached Laplace Transform Table. Hint:

The Laplace transform of $\frac{d\delta(t)}{dt}$ is s . 5 Marks

$f(t)$	$F(s)$
1	$\frac{1}{s}$
δ	1
$\delta^{(k)}$	s^k
t	$\frac{1}{s^2}$
$\frac{t^k}{k!}, k \geq 0$	$\frac{1}{s^{k+1}}$
e^{at}	$\frac{1}{s - a}$
$\cos \omega t$	$\frac{s}{s^2 + \omega^2} = \frac{1/2}{s - j\omega} + \frac{1/2}{s + j\omega}$
$\sin \omega t$	$\frac{\omega}{s^2 + \omega^2} = \frac{1/2j}{s - j\omega} - \frac{1/2j}{s + j\omega}$

2.2. $F(s) = \frac{s^2 + 2s + 3}{(s+1)^3}$ 5 Marks

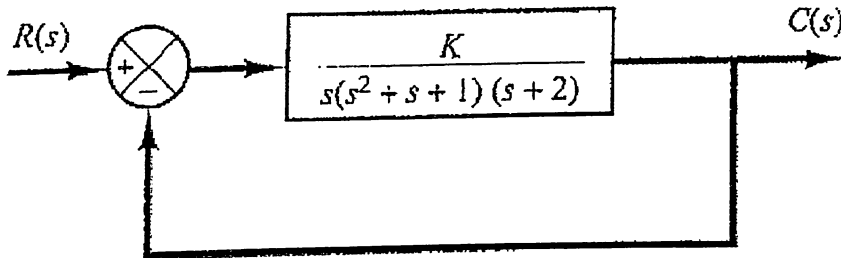
Question 3. Discuss the following topics related to First Order Systems based on their specific block diagrams:

3.1. Draw the complete and simplified block diagrams and discuss Unit-Step Response of First Order Systems **5 Marks**

3.2. Draw the complete and simplified block diagrams and discuss Unit Impulse Response of First Order Systems **5 Marks**

Question 4. Consider the system shown below. Determine the range of parameter K for stability using Routh's Criterion.

10 Marks



Hints:

$$\frac{C(s)}{R(s)} = \frac{b_0s^m + b_1s^{m-1} + \dots + b_{m-1}s + b_m}{a_0s^n + a_1s^{n-1} + \dots + a_{n-1}s + a_n} = \frac{B(s)}{A(s)}$$

$$b_1 = \frac{a_1a_2 - a_0a_3}{a_1}, b_2 = \frac{a_1a_4 - a_0a_5}{a_1}, \frac{b_1a_3 - a_1b_2}{b_1}, c_2 = \frac{b_1a_5 - a_1b_3}{b_1}, d_1 = \frac{c_1b_2 - b_1c_2}{c_1}.$$

Marking Criteria:

Criterion Weighting	Exemplary, 85%-100%	Highly Accomplished, 75%-84%	Accomplished 65%-74%,	Satisfactory 50%-64%	Unsatisfactory, <50%	Marks Awarded
Structure, Effective and Inclusive Language, Grammar, Spelling, Punctuation, Style. 20						
Clear and Complete Definitions, 20						
Correctness of Solutions with Diagrams and Demonstrations, 40						
Discussions and Conclusions, 20						